

# Some of my advanced original problems

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A11. Let  $(x_n)$  and  $(y_n)$  be a sequence of real numbers such that for every

Prove that

A10. For every real number  $\epsilon$  define  $f_\epsilon$  by the relation

Prove that  $f_\epsilon$  is a well defined integrable function, then compute

A9. Let  $f$  and  $g$  there be given and the inequality

Prove that:

(i) If  $f$  holds whenever then

(ii) If  $g$  holds whenever then

A8. Find  $\xi$  with the intermediate value property such that

A7. Solve  $\sin x = x$  in real numbers:

A6. Find all derivable functions  $f$  such that

A5. Let  $f_n$  be linear on each interval  $[n, n+1]$  such that for every integer  $n$  with  $f_n(n) = n$ . Prove that  $f$  is antiderivable.

A4. Let  $A, B$  be matrices with real entries such that  $A^2 = B^2$ . Prove that

A3. Let  $A, B$  be matrices with complex entries such that  $A^2 = B^2$ . Prove that  $A = B$  or

A2. Let  $a, b$  be elements of a ring  $R$ ,  $a$  invertible, such that

whenever  $a \mid b$ . Prove that

A1. Let  $f$  be continuous such that for every reals  $x, y$ , there exist  $\xi, \eta$  such that

Prove that  $f$  is nondecreasing.

